

$$\text{Mean} \Rightarrow \bar{x} = \frac{\sum x_i}{n} \quad \text{standard deviation} \Rightarrow s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

$$\text{Confidence interval: } \mu = \bar{x} \pm \frac{ts}{\sqrt{n}} \quad \% e = \frac{e}{\bar{x}} \cdot 100$$

$$\pm t = (\bar{x} - \mu) \left(\frac{\sqrt{n}}{s} \right) \quad \text{CASE 1}$$

$$t = \frac{|\bar{x}_1 - \bar{x}_2|}{s_{\text{pooled}}} \sqrt{\frac{n_1 n_2}{n_1 + n_2}} \quad s_{\text{pooled}} = \sqrt{\frac{s_1^2(n_1-1) + s_2^2(n_2-1)}{n_1 + n_2 - 2}} \quad \text{Case 2}$$

$$t = \frac{\bar{d}}{s_d} \sqrt{n} \quad s_d = \sqrt{\frac{\sum (d_i - \bar{d})^2}{n-1}}$$

$$Q = \frac{\text{gap}}{\text{range}} \quad F = \frac{s_1^2}{s_2^2} \quad e_f = \sqrt{\sum_{i=1}^n e_i^2} \quad \% e_f = \sqrt{\sum_{i=1}^n \% e_i^2}$$

$$\frac{\text{concentration ratio (x/s) in unknown}}{\text{concentration ratio in standard mixture}} = \frac{\text{signal ratio (x/s) in unknown}}{\text{signal ratio in standard mixture}}$$

INTERNAL STANDARD

$$\frac{[X]_i}{[X]_f + [S]_f} = \frac{[I]_x}{[I]_{x+s}}$$


$$\frac{[x]}{[is]} \cdot F = \frac{I_x}{I_{is}}$$

$$A = \log_{10}(P_0/P) = -\log_{10} T$$

$$\text{Grating Equation: } n\lambda = d(\sin\theta - \sin\phi)$$

$$A = \varepsilon b C \quad C = \lambda v,$$

$$E = h\nu \quad E = (-2.178 \times 10^{-18} \text{ J}) * (z^2/n^2)$$

$$N = \frac{16 t_r^2}{W^2} \text{ or } \frac{5.55 t_r^2}{W_{1/2}^2} \quad R = \frac{\Delta t_r}{W_{av}}$$

TABLE 3-1 Summary of rules for propagation of uncertainty

Function	Uncertainty	Function ^a	Uncertainty ^b
$y = x_1 + x_2$	$e_y = \sqrt{e_{x_1}^2 + e_{x_2}^2}$	$y = x^a$	$\%e_y = a\%e_x$
$y = x_1 - x_2$	$e_y = \sqrt{e_{x_1}^2 + e_{x_2}^2}$	$y = \log x$	$e_y = \frac{1}{\ln 10} \frac{e_x}{x} \approx 0.43429 \frac{e_x}{x}$
$y = x_1 \cdot x_2$	$\%e_y = \sqrt{\%e_{x_1}^2 + \%e_{x_2}^2}$	$y = \ln x$	$e_y = \frac{e_x}{x}$
$y = \frac{x_1}{x_2}$	$\%e_y = \sqrt{\%e_{x_1}^2 + \%e_{x_2}^2}$	$y = 10^x$	$\frac{e_y}{y} = (\ln 10)e_x \approx 2.3026 e_x$
		$y = e^x$	$\frac{e_y}{y} = e_x$

a. x represents a variable and a represents a constant that has no uncertainty.

b. e_x/x is the relative error in x and $\%e_x$ is $100 \times e_x/x$.

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general : $e_f = \sqrt{\sum_i \left(\frac{\partial f}{\partial x_i} \right)^2 \cdot e_i^2}$

TABLE 4-2 Values of Student's t

Degrees of freedom	Confidence level (%)						
	50	90	95	98	99	99.5	99.9
1	1.000	6.314	12.706	31.821	63.656	127.321	636.578
2	0.816	2.920	4.303	6.965	9.925	14.089	31.598
3	0.765	2.353	3.182	4.541	5.841	7.453	12.924
4	0.741	2.132	2.776	3.747	4.604	5.598	8.610
5	0.727	2.015	2.571	3.365	4.032	4.773	6.869
6	0.718	1.943	2.447	3.143	3.707	4.317	5.959
7	0.711	1.895	2.365	2.998	3.500	4.029	5.408
8	0.706	1.860	2.306	2.896	3.355	3.832	5.041
9	0.703	1.833	2.262	2.821	3.250	3.690	4.781
10	0.700	1.812	2.228	2.764	3.169	3.581	4.587
15	0.691	1.753	2.131	2.602	2.947	3.252	4.073
20	0.687	1.725	2.086	2.528	2.845	3.153	3.850
25	0.684	1.708	2.060	2.485	2.787	3.078	3.725
30	0.683	1.697	2.042	2.457	2.750	3.030	3.646
40	0.681	1.684	2.021	2.423	2.704	2.971	3.551
60	0.679	1.671	2.000	2.390	2.660	2.915	3.460
120	0.677	1.658	1.980	2.358	2.617	2.860	3.373
∞	0.674	1.645	1.960	2.326	2.576	2.807	3.291

In calculating confidence intervals, σ may be substituted for s in Equation 4-6 if you have a great deal of experience with a particular method and have therefore determined its "true" population standard deviation. If σ is used instead of s , the value of t to use in Equation 4-6 comes from the bottom row of Table 4-2.

Values of t in this table apply to two-tailed tests illustrated in Figure 4-9a. The 95% confidence level specifies the regions containing 2.5% of the area in each wing of the curve. For a one-tailed test, we use values of t listed for 90% confidence. Each wing outside of t for 90% confidence contains 5% of the area of the curve.

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TABLE 4-5 Critical values of G for rejection of outlier

Number of observations	G (95% confidence)
4	1.463
5	1.672
6	1.822
7	1.938
8	2.032
9	2.110
10	2.176
11	2.234
12	2.285
15	2.409
20	2.557

$$G_{\text{CAL}} = \frac{|out - \bar{x}|}{S}$$

$G_{\text{calculated}} = |\text{questionable value} - \text{mean}|/s$. If $G_{\text{calculated}} > G_{\text{table}}$, the value in question can be rejected with 95% confidence. Values in this table are for a one-tailed test, as recommended by ASTM.

SOURCE: ASTM E 178-02 Standard Practice for Dealing with Outlying Observations, <http://webstore.ansi.org>; F. E. Grubbs and G. Beck, *Technometrics* 1972, 14, 847.

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R.W. Parker

Of The Elements

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64 3539 1585 7.89 Gadolinium 157.25 ±3	+3 3496 1630 8.27 Terbium 158.925 34 ±2	65 2835 1682 8.54 Dysprosium 162.50 ±3	+3 2968 1743 8.80 Holmium 164.930 32 ±2	66 3136 1795 9.05 Erbium 167.26 ±3	+3 2220 1818 9.33 Thulium 168.934 21 ±2	67 3136 1795 9.05 Erbium 167.26 ±3	+3.2 2220 1818 9.33 Thulium 168.934 21 ±2	68 3136 1795 9.05 Erbium 167.26 ±3	+3.2 2220 1818 9.33 Thulium 168.934 21 ±2	69 3136 1795 9.05 Erbium 167.26 ±3	+3.2 2220 1818 9.33 Thulium 168.934 21 ±2	70 1467 1097 6.98 Ytterbium 173.04 ±3	+3.2 2220 1818 9.33 Thulium 168.934 21 ±2	71 3668 1936 9.84 Lutetium 174.967
96 1340 13.51 Curium (247)	+3 97 Berkelium (247)	97 +4.3 Berkelium (247)	98 900 Californium (251)	99 Cf ⁵ Einsteinium (254)	100 Es Fermium (257)	101 Fm Mendelevium (260)	102 Md Nobelium (259)	103 No Lawrencium (262)	104 Lr Lawrencium (262)	105 Lr Lawrencium (262)	106 Lr Lawrencium (262)	107 Lr Lawrencium (262)	108 Lr Lawrencium (262)	109 Lr Lawrencium (262)